## Problem Set 9

[Your name] and [student ID]
MAT1841-2021

Problem 1 ( 40 points). Let $X$ be a finite set of points in some Euclidean space and let $r \geq 0$. Prove that $V R(X, r) \subset C e c h(X, \sqrt{2} r)$.

Problem 2 ( 30 points). If $K$ is a p-dimensional simplicial complex and for each $k, n_{k}$ is the number of $k$-simplices in $K$, then the Euler number of $K$ is given by

$$
\chi(K)=\sum_{k=0}^{p}(-1)^{p} n_{p} .
$$

Direclty show that any two triangulations of the circle $S^{1}$ have the same Euler number.
Problem 3 ( 30 points). Construct a simplicial complex with $\beta_{2}=3, \beta_{1}=2, \beta_{0}=1$. Prove your construction is correct.

