Modular arithmetic computations review Lecture 7b: 2022-03-02

MAT A02 – Winter 2022 – UTSC Prof. Yun William Yu

General rules for congruence class

• $a \equiv b \pmod{n} \leftrightarrow a - b \equiv 0 \pmod{n}$, which is to say that a and b differ by a multiple of n.

• To find the smallest positive label for $a \pmod{n}$, simply find the remainder of $a \div n$.

Adding in modular arithmetic

- When adding $a + b \pmod{n}$, two options:
 - (1) Add the two numbers in normal arithmetic first, and then divide to find the smallest positive label.

• (2) Replace the two numbers with another number from their respective congruence classes first, then add, and then replace again.

Multiplying in modular arithmetic

- When multiplying $a \times b \pmod{n}$, two options:
 - (1) Multiply the two numbers in normal arithmetic first, and then divide to find the smallest positive label.

• (2) Replace the two numbers with another number from their respective congruence classes first, then multiply, and then replace again. (sometimes helpful to use negatives)

Simple powers in modular arithmetic

• To compute powers, sometimes it is easier to break it up into a product and simplify.

• 637 × 437 (mod 7)

• 507 × 237 (mod 509)

• 367² (mod 369)

• $7^6 \pmod{51}$

A: 0 B: 4 C: 35 D: 43 E: None of the above

• 432903 + 1463974 (mod 100)

• 105 × 237 (mod 7)

• $4502^2 \pmod{4507}$

• $76 \times 77 \times 78 \pmod{79}$

A: 0 B: 25 C: 73 D: 77 E: None of the above

• 3⁶⁴ (mod 78)

- A: 3 B: 6
- C: 9
- D: 27
- E: None of the above

• 3⁶⁴ (mod 25)

- A: 3 B: 6
- C: 9
- D: 27
- E: None of the above